SBML Protocol for Conquering Simultaneous Failures with Group Dissemination Functionality*

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This paper presents a new sender based message logging (SBML) protocol to tolerate simultaneous failures by using the beneficial features of FIFO group communication links effectively. The protocol can lift the inherent weakness of the original SBML by replicating the log information of each message sent to a process group into the volatile storages of its members. Therefore, even if only one process in a group survives at a time, our protocol can progress the execution of the entire system without stopping and restarting it. Also, it needs no extra control message by piggybacking the additional information on the control message for logging every previous protocol essentially requires. The experimental results show our protocol can be a low cost solution for addressing the important drawback of the original SBML based on group communication without RSN replication functionality.

Keywords: distributed system, simultaneous failure, group communication, message logging, rollback recovery

1. INTRODUCTION

As the scale and the complexity of distributed and parallel applications rapidly grow in an unprecedented pace, the research on developing large-scale distributed computing system platforms is gaining a big attention in various application fields such as cloud computing, social networks, unmanned aerial systems, disaster recovery, smart power grid, and so on [14, 15, 20, 22-24]. These platforms should provide the users with an optimized and on-demand composition of services using highly dynamic, asynchronous, and geographically dispersed resources in a transparent way unlike the previous ones. A large-scale platform, that utilizes many low cost but powerful commodity computing devices, may have a higher chance of a failure as its components are more likely to crash than in small-scale platforms [1, 4, 8, 13, 16, 18]. Thus, fault-tolerance techniques should be employed to reduce the wasted execution time. For this purpose, one of two methods can be used, that is, 1) process replication, or 2) log-based rollback recovery. But the first method may degrade the scalability of the platform significantly due to its high overhead of synchronization among the replicated processes [9]. Therefore, in this paper, we focus on the second method, i.e., log-based rollback recovery, due to its low overhead.

Among the log-based recovery techniques [1, 2, 6, 12, 17, 26, 29], the sender-based message logging (SBML) with checkpointing [3, 10, 14, 25] is used commonly as a low-cost transparent rollback recovery technique in many fields such as mobile computing, cluster and grid computing, sensor network, and so on. This popularity is due to no

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need for specialized hardware and a considerably low overhead for synchronous logging on a stable storage by using volatile logging at sender's memory [3, 10, 14, 25]. However, every previous SBML protocol has the restriction that they can tolerate only a single failure at one time, called sequential failures. Thus, even if the protocol has been executed, simultaneous failures may cause the system inconsistency problem [10, 29].

As group-based computing has prevailed as a general model of current and future generation computing, multicast communication is becoming a mandatory building block for this computing. However, as all the existing SBML protocols have assumed reliable FIFO point-to-point communication links, they may not effectively employ log information of the same message to a process group its members received if they are applied into group communication link-based distributed system platforms. This paper presents a new sender-based message logging protocol to tolerate simultaneous failures by using the beneficial features of group communication links effectively. In order to address the critical weakness of the previous protocols, the proposed protocol makes every process know the respective receive sequence number of each same message to every other live group member by saving the number from the sender of the message onto its own volatile memory. This feature enables the protocol to survive a number of simultaneous failures except the whole system failure. Also, it needs no extra control message by piggybacking the additional information on the control message for logging every previous protocol essentially requires.

The remainder of the paper is structured as follows. In section 2, we describe the distributed system model assumed and, in section 3, the limitation of the previous SBML in detail. Section 4 introduces our SBML protocol and section 5 shows its correctness proof. In sections 6 and 7, we analyze and evaluate our protocol over the original one and, in section 8, conclude this paper.

2. SYSTEM MODEL

A distributed computation consists of a set P of n(n > 0) sequential processes executed on nodes in the system and there is a distributed stable storage that every process can always access that persists beyond processor failures, thereby supporting recovery from failure of an arbitrary number of processors [9]. Processes have no global memory and global clock. The system is asynchronous: each process is executed at its own speed and communicates with each other only through messages at finite but arbitrary transmission delays. Exchanging messages may temporarily be lost but, eventually delivered in FIFO order. We assume that the communication network is immune to partitioning and nodes fail according to the fail stop model where every crashed process on them halts its computation with losing all contents of its volatile memory [19]. Events of processes occurring in a failure-free execution are ordered using Lamport’s happened before relation [11]. →hb, defined by the following three conditions. Let p, q and r be three processes ∈ P and ekp be the k-th event of p (k > 0):

- If ep^i and eq^j occur, p=q and i<j, then ep^i →hb eq^j.
• If $e_p^i$ is the event that $p$ sends a message to $q$, $e_q^j$ is the event that $q$ receives the message from $p$ and then delivers it to the application, and $p \neq q$, then $e_p^i \rightarrow ^{hb} e_q^j$.

• If $e_p^i \rightarrow ^{hb} e_q^j$ and $e_q^j \rightarrow ^{hb} e_t^k$, then $e_p^i \rightarrow ^{hb} e_t^k$.

The main goal of log-based rollback recovery is to bring the system to a failure-free state when inconsistencies occur due to failures. The execution of each process is piece-wise deterministic [7, 21]: at any point during the execution, a state interval of the process is determined by a non-deterministic event, which is delivering a received message to the appropriate application. The k-th state interval of process $p$, denoted by $s^k_p(k > 0)$, is started by the delivery event of the k-th message $m$ of $p$, denoted by $dev^k_p(m)$. Therefore, given $p$‘s initial state, $s^0_p$, and the non-deterministic events, $[dev^1_p, dev^2_p, ..., dev^l_p]$, its corresponding state $s^1_p$ is uniquely determined. Let $p$‘s state, $s^1_p = [s^0_p, s^1_p, ..., s^j_p]$, represent the sequence of all state intervals up to $s^j_p$. $s^j_p$ and $s^j_q(p \neq q)$ are mutually consistent if all messages from $q$ that $p$ has delivered to the application in $s^j_p$ were sent to $p$ by $q$ in $s^j_q$, and vice versa [5]. A set of states, which consists of only one state for every process in the system, is a globally consistent state if any pair of the states is mutually consistent.

To understand these definitions precisely, Fig. 1 shows two examples of global states, which are shown by broken arrows. In Fig. 1(a), states $s^j_p$ and $s^j_q$ are mutually consistent because they reflect sending and receiving message $m^1$ respectively. Message $m^2$ has been sent in state $s^j_q$ but not yet received in state $s^j_r$. The states $s^j_q$ and $s^j_r$ are also mutually consistent because the situation where the message $m^2$ has been in transit could have occurred in a failure-free and correct execution. We call such a message an in-transit message. Therefore, the global state in this figure, consisting of $s^j_p$, $s^j_q$, and $s^j_r$, is consistent. However, in Fig. 1(b), states $s^1_p$ and $s^1_q$ are mutually inconsistent because though message $m^1$ has not been left in the state $s^1_p$, the state $s^1_q$ has reflected receiving the message. Such a message like $m^1$ is named orphan message. Here, orphan message means the message received from a process though there is no record that it was sent from the process due to process failures. Message $m^2$ may make the state of $q$, $s^2_q$, inconsistent with those of the other live processes after recovery. At this time, the receiver of $m^1$, $q$, is called orphan process. Thus, the states, $s^1_p$, $s^1_q$, and $s^1_r$, in this figure compose a globally inconsistent state. In conclusion, we can redefine a globally consistent state as follows.

**Definition 1.** A global state $S$ is consistent if and only if there arises no orphan message in the state.

In the remainder of this paper, the messages applications generate are called application messages and the messages used for the message logging and recovery procedures, control messages.
3. BACKGROUND

Before introducing our proposed SBML protocol to be capable of overcoming the limitations of the previous SBML, let us identify the exact reasons why the latter has its incapability against tolerating simultaneous failures based on both unicast and group communication links using some examples. Originally, sender-based message logging [10] is designed to have the positive feature of receiver-based pessimistic message logging [17, 26], no roll-back property, in case of sequential failures. Also, it may significantly reduce the high failure-free overhead resulting from the disadvantageous feature of the latter, i.e., synchronous logging on stable storage as soon as each message is received or before any message, generated after the received message, is sent to another process. To satisfy these requirements, this technique allows each received message to be logged on the volatile storage of its sender, called semi-synchronous logging. Also, to ensure system consistency in case a process crashes at a time, the log information of each message received by the process is forced to save into its sender's volatile storage before sending another process any message generated after the receipt of the former message.

Let us closely examine how sender-based message logging can have the feature mentioned above using Fig. 2. In the figure, three processes, p0, p1, and p2, execute their respective computation together by exchanging messages with each other. Processes p0 and p2 send messages m₁ and m₂ to process p1 respectively. In this operation, each sender records the partial log information of the corresponding sent message on its own volatile memory. At this point, the log information of a message m is denoted by SLog(m), which is composed of four elements, the send sequence number (SSN), the receive sequence number (RSN), the receiver's id (RID) and data of the message [10, 21, 25, 29]. Here, partially logged means the RSN of the message has not been recorded on SLog(m) yet. Then, p1 first receives message m₁ from p0, increments its RSN, RSN₁, by one, and...
assigns the value of $RSN_1 (= \alpha)$ to the message. Next, $p_1$ sends sender $p_0$ an acknowledgment message including $m_1$’s RSN. Similarly, when $p_1$ receives $m_2$ from $p_2$, it performs the same procedure, where the assigned value of $m_2$’s RSN is $(\alpha+1)$ in this example. When each sender, e.g., $p_0$ or $p_2$, obtains an acknowledgment message for its sent message $m$, e.g., $m_1$ or $m_2$, from the corresponding receiver, it saves $m$’s RSN attached to the acknowledgment into $m$’s log information, $SLog(m)$. At this time, $m$ is called fully logged, meaning every element in $SLog(m)$ is filled with its actual value for $m$’s recovery. Then, the sender notifies $p_1$ of the fact that it safely holds the full log information on its own volatile memory. So, even if $p_1$ fails afterwards, it can get the full log information for $m_1$ and $m_2$ from the two senders respectively and replay them in the same order like in the pre-failure state. Therefore, even though there have been any messages sent from $p_1$ after $m_1$ and $m_2$ in this case, they would not become orphan messages.

Let us consider what happens when several processes fail at the same time using Fig. 3. This figure shows an execution similar to the one in Fig. 2 except that $p_3$ joins the execution and sends the third message $m_3$ to $p_1$. After all the logging procedures for the three messages have been completed, $p_1$ transmits message $m_4$ to $p_2$. Then, suppose the three processes $p_0$, $p_1$ and $p_3$ crash simultaneously. In this case, as $p_0$ and $p_3$ lost the values of the RSNs of messages $m_1$ and $m_3$ on their respective volatile memories due to the failures, they cannot provide the RSN values for $p_1$ during recovery. Also, $p_2$ has only the value of $m_2$’s RSN. This log information deficiency causes the following ambiguous situation: $p_1$ cannot determine in which order $m_1$, $m_2$ and $m_3$ should be replayed. Thus, $p_1$ may not reconstruct message $m_4$ during recovery, which makes $p_2$ orphan process. Due to this incapability, every previous sender-based message logging may not make sure the entire system consistency on simultaneous failure occurrences. However, if unicast-only communication links are assumed in the system model, this technique would be unavoidably destined to this limitation without the help of any other compensating methods [10, 29].
Suppose group dissemination functionality is the basic communication feature of the system. With this assumption, we could naively anticipate p1 can get m1’s RSN from p2 even if both p0 and p1 crash simultaneously in Fig. 2 because p2 also received m1 sent to the group consisting of p0, p1 and p2. Let us identify that the original SBML can satisfy this expectation using Fig. 4. In reality, actual process group size may vary depending on application types, but for the sake of simplicity of explanation, we assume a very small group in the examples used later. In the figure, there are three processes, p0, p1 and p2, composing a process group g, and there are three messages, m01, m02 and m03, sent to group g from senders S1, S2 and S3 respectively. Here, assume each sender may also be a member of group g. In this example, suppose the RSNs of p0, p1 and p2 be (α-1), (β-1), (γ-1) (α ≠ β ≠ γ) in order before sending out the three messages. Here, all three messages will eventually be delivered to every process member through reliable FIFO group communication links, but the RSNs of each message assigned by all three processes may all be different due to delivery order asynchrony of messages sent to a group from different senders. In this example, p0, p1 and p2 receive m1, m2 and m3, m2, m1 and m3, m1 and m2 in order, respectively. In this case, the RSNs they have assigned to m1 could be α, β+2 and γ+1 like in this figure. Thus, if the sender of m1, S1, and p0, p1 crash at the same time, m1 may not be replayed with its pre-failure RSN value, α, at p0 during recovery.

For example, Fig. 5 shows the case that the senders of the three messages are p0, p1 and p2 respectively. Here, p0 receives m1, m2 and then m3 whose RSNs become each α, (α+1) and (α+2). Similarly, p1 assigns β, (β+1) and (β+2) as RSN to m2, m1 and m3 and p2 assigns γ, (γ+1) and (γ+2), m1, m2 and m3. Afterwards, every message receipt event on each process in this figure triggers the semi-synchronous logging procedure for the corresponding message like in Fig. 2. Hereafter, suppose p0 or p1 crash at the same time. During recovery, they can get the values of m1’s RSNs from p0, (α+2), (β+1) and γ, assigned by each process, but no information about the values of m1’s and m2’s RSNs they allocated in the pre-failure state. Thus, neither p0 nor p1 can decide in which order the three messages should be replayed. If there were any messages either p0 or p1, or both sent to p2 after the completion of logging m1, m2 and m3 before their failures, p2 might be an orphan process after performing the recovery procedure of the original SBML.
SBML PROTOCOL FOR CONQUERING SIMULTANEOUS FAILURES WITH GROUP DISSEMINATION

Fig. 4. Limitation of the original SBML based on reliable FIFO group communication links.

Fig. 5. An execution case showing the inconsistency problem the original SBML based on group dissemination links may incur in case of simultaneous failures.
4. NOVEL SBML PROTOCOL

From the observation, it is found out that as the original sender-based message logging has been developed assuming reliable FIFO unicast communication functionality, it could not utilize the advantageous features of the group communication functionality, which may potentially make a breakthrough to overcome its annoying constraint. Thus, our SBML protocol is designed to have the following beneficial features to address it;

- Replicate the RSN information of a message sent to a group, separately assigned by each member, into volatile storages of other group members.
- Force the state made after each message multicast to a group to be unable to be visible to any other process until the replication has been completed.

With these features, the protocol can tolerate simultaneous failures while it attempts to minimize additional inter-process communication cost required for no rollback of live processes by piggybacking the additional information on the control message for logging every previous protocol essentially needs. For this purpose, the data structures each group member should maintain in our protocol are following;

- \( \text{SSN}_g^i \): the send sequence number of the latest message sent by \( p_g^i \).
- \( \text{RSN}_g^i \): the receive sequence number of the latest message delivered to \( p_g^i \).
- \( \text{SSNV}_g^i \): a vector where \( \text{SSNV}_g^i[q] \) is the ssn of the last message that was delivered to \( p_g^i \) from a process \( p_g^q \).
- \( \text{XSLog}_g^i \): a set saving \( e(gid, ssn, rsnlist, data) \) of each message sent by \( p_g^i \). Here, \( e \) is the log information of a message and the first two fields and the last field are the identifier of the process group, the send sequence number and data of the message respectively. The third field is the list of receive sequence numbers of the message which all receivers of the message assigned to it. Its element consists of a pair of \( (pid, rsn) \), where \( pid \) is one of the receivers and \( rsn \) is the rsn of the message \( pid \) assigns to it.
- \( \text{XRLog}_g^i \): a set which maintains \( e(sid, ssn, rsnlist) \) of each message received by \( p_g^i \). Here, \( e \) is the log information of the message and the first two fields are the sender's id and the send sequence number of the message respectively. The last field is a set of elements whose form is \( (pid, rsn) \) where \( pid \) is one of group members including \( p_g^i \) that has assigned rsn as RSN to the message on its receipt. This set can help other crashed group members perform replaying the message in their pre-failure orders with its corresponding rsn.
- \( \text{stableRSN}_g^i \): the receive sequence number of the latest message which has been delivered to \( p_g^i \) and replicated on the volatile storage of every member or checkpointed on the stable storage. It is used for indicating until which messages \( p_g^i \) can send to other processes.

In order to satisfy the requirements mentioned above, our protocol is performed as follows. For this purpose, let us closely look at an example showing the detail of execution of the protocol. This example is the same as that of Fig. 5. In Fig. 6, processes \( p_g^0 \), \( p_g^1 \) and \( p_g^2 \), multicast three messages, \( m^1 \), \( m^2 \) and \( m^3 \), to every member of group \( g \) includ-
ing itself respectively. Here, $p_0^s$ receives $m^1$, $m^2$ and then $m^3$ whose RSN values become $\alpha$, $(\alpha+1)$ and $(\alpha+2)$ in order. When $p_1^s$ receives $m^2$, $m^3$ and $m^1$ in order, it assigns $\beta$, $(\beta+1)$ and $(\beta+2)$ as RSN to them respectively. Similarly, after $p_2^s$ has received $m^3$, $m^1$ and $m^2$ in order, their RSNs become $\gamma$, $(\gamma+1)$ and $(\gamma+2)$ respectively. All the three processes execute the proposed protocol like in Fig. 7. For simplicity, this figure only shows the case $p_0^s$ disseminates $m^1$ to every group member including itself. First, after sending $m^1$, $p_0^s$ saves the partial log element $(\text{tag}^1, \emptyset, \text{data}_m)$ into $\text{XSLog}^0$ in procedure Module $\text{G-SEND(data}_m, g)$ in Fig. 8. When having received $m^1$, $p_0^s$, $p_1^s$ and $p_2^s$ add their respective receiver log elements, $(\text{tag}^1, \{(p_0^s, \alpha)\})$, $(\text{tag}^1, \{(p_1^s, \beta+2)\})$ and $(\text{tag}^1, \{(p_2^s, \gamma+1)\})$, to $\text{XRLog}^0_1$, $\text{XRLog}^1_0$ and $\text{XRLog}^1_0$ in Module $\text{G-RECV(tag}^1, \text{data}_m)$. Then, they send each an acknowledgment, $\text{rsn-return}((\text{tag}^1, \alpha)$, $\text{rsn-return}((\text{tag}^1, \beta+2)$ and $\text{rsn-return}((\text{tag}^1, \gamma+1)$, to $m^1$'s sender $p_0^s$. When $p_0^s$ receives the three return messages in a particular order, it inserts its RSN elements, $(p_0^s, \alpha)$, $(p_1^s, \beta+2)$ and $(p_2^s, \gamma+1)$, into $\text{XSLog}^0$ in Module $\text{RCV-RSN(tag}^1, \text{RSN}_m)$. When $p_0$ has collected each an acknowledgment from every live group member, it multicasts a control message including the value of the RSN of $m^1$ assigned by the member, e.g., $\{(p_0^s, \alpha), (p_1^s, \beta+1), (p_2^s, \gamma)\}$, to the group. When the control message has arrived, $p_0^s$, $p_1^s$ and $p_2^s$ update their receiver logs, $\text{XRLog}^0_0$, $\text{XRLog}^1_0$ and $\text{XRLog}^1_0$, with the list of RSNs piggybacked on the message in Module $\text{RCV-ACK(tag}_2^1, \text{RSN}_m)$. In Fig. 6, $m^1$ and $m^2$ also experience the same logging procedures as those of Fig. 7. In this way, after our protocol has been completed with the three messages, every group member can maintain the values of all the RSNs assigned to each message by the member, e.g., $\{(p_0^s, \alpha), (p_1^s, \beta+2), (p_2^s, \gamma+1)\}$, $(\text{tag}^2, \{\{p_0^s, \alpha+1\}, (p_1^s, \beta), (p_2^s, \gamma+2)\})$ and $(\text{tag}^2, \{\{p_0^s, \alpha+2\}, (p_1^s, \beta+1), (p_2^s, \gamma)\}$, on its volatile memory.

![Fig. 6. Illustration showing how our SBML protocol can effectively address simultaneous failures.](image-url)

Thanks to this log information replication, even though $p_0^s$ and $p_1^s$ fail at the same time in Fig. 6, they trigger Module $\text{RECOVERY()}$ in Fig. 8 to be able to obtain their
own RSN values for every received message from Module RCVRQTRCVY(p₀^2) of p₂ during recovery. Then, p₀ can deterministically replay m₁, m₂ and m₃ in order, and p₁, m₁, m₂, and m₃ like before failure. Therefore, even if p₀ or p₁ transmitted any message to p₂ after m₁, m₂ and m₃ in its pre-failure state, p₂ would not be orphan process after recovery.

The algorithmic description of message logging and recovery procedures of our protocol is shown in Fig. 8 and 9.

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### Fig. 7
An illustration showing the detail of our SBML protocol based on group dissemination links with message m₁ multicast to group g from process p₀.

<table>
<thead>
<tr>
<th>XRLog₀^₀</th>
<th>XSLog₀^₀</th>
</tr>
</thead>
<tbody>
<tr>
<td>(2) {(tag₀¹,{(p₀⁰,α)})}</td>
<td>(1) {(tag₀¹,∅,dataₘ₁)}</td>
</tr>
<tr>
<td>(3) {(tag₀¹,{(p₀⁰,α),(p₀¹,β+2),(p₀²,γ+1)})}</td>
<td>(2)-(2)'' {(tag₀¹,{(p₀⁰,α),(p₀¹,β+2),(p₀²,γ+1)},dataₘ₁)}</td>
</tr>
</tbody>
</table>

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### After Step 1 of p₀^₀
RSN₀¹ = α-1 → α
XRLog₀¹ = {(tag₀¹,((p₀ⁿ,α)))}

### After (1) of p₀^₁
RSN₀¹ = β+1 → β+2
XRLog₀¹ = {(tag₀²,((p₀ⁿ,β+2)))}

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### After (1) of p₀^₂
RSN₀² = γ → γ+1
XRLog₀² = {(tag₀²,((p₀ⁿ,γ+1)))}

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### XRLog¹^₀
(2)' {(tag₁¹,((p₁ⁿ,β+2)))}
(3) {(tag₁¹,((p₁⁰,α),(p₁¹,β+2),(p₁²,γ+1)))}

### XSLog¹^₀
(1) {(tag₁¹,∅,dataₘ₁)}
(2)-(2)'' {(tag₁¹,((p₁⁰,α),(p₁¹,β+2),(p₁²,γ+1)),dataₘ₁)}

### XRLog¹^₁
(2)' {(tag₁¹,((p₁ⁿ,β+2)))}
(3) {(tag₁¹,((p₁⁰,α),(p₁¹,β+2),(p₁²,γ+1)))}

### XSLog¹^₁
(1) {(tag₁¹,∅,dataₘ₁)}
(2)-(2)'' {(tag₁¹,((p₁⁰,α),(p₁¹,β+2),(p₁²,γ+1)),dataₘ₁)}

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### XRLog¹^₂
(2)' {(tag₁¹,((p₁ⁿ,β+2)))}
(3) {(tag₁¹,((p₁⁰,α),(p₁¹,β+2),(p₁²,γ+1)))}

### XSLog¹^₂
(1) {(tag₁¹,∅,dataₘ₁)}
(2)-(2)'' {(tag₁¹,((p₁⁰,α),(p₁¹,β+2),(p₁²,γ+1)),dataₘ₁)}

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// When process \( p_{gid}^i \) attempts to multicast a message \( m \) including data to every member of group \( g \). //
Module G-SEND(data, gid) AT \( p_{gid}^i \)
  \( SSN_{gid}^i \leftarrow SSN_{gid}^i + 1 \); \textbf{multicast} \( m(p_{gid}^i, SSN_{gid}^i, \text{data}) \) to group \( g \);
  \( XSLog_{gid}^i \leftarrow XSLog_{gid}^i \cup \{(gid, SSN_{gid}^i, \emptyset, \text{data})\}; \)

// When process \( p_{gid}^i \) receives a message \( m \) from message sender \( m.sndr \). //
Module G-RECV(m(sndr, ssn, data)) AT \( p_{gid}^i \)
  if(\( SsnVt_{gid}^i[m.sndr] < m.ssn \)) then
    \( RSN_{gid}^i \leftarrow RSN_{gid}^i + 1 \);
    \( SsnVt_{gid}^i[m.sndr] \leftarrow m.ssn \);
    \( send \ rsn-return(p_{gid}^i, m.ssn, RSN_{gid}^i) \) to \( m.sndr \);
    \( XRLog_{gid}^i \leftarrow XRLog_{gid}^i \cup \{(m.sndr, m.ssn, \{(p_{gid}^i, RSN_{gid}^i)\})\}; \)
  else
    \( find \ \exists e \in XRLog_{gid}^i \) \( st \ (e.sndr = m.sndr) \wedge (e.ssn = m.ssn) \);
    \( find \ \exists o \in e.rsnlist \) \( st \ (o.rcvr = p_{gid}^i) \);
    \( send \ rsn-return(p_{gid}^i, m.ssn, o.rsn) \) to \( m.sndr \);

// When message sender \( p_{gid}^i \) receives a message \( rsn \)-return from the receiver \( rsn-return.rcvr \) of a message whose \( rsn \) value is \( rsn-return.rsn \). //
Module RCV-RSN(rsn-return(rcvr, ssn, rsnlist)) AT \( p_{gid}^i \)
  \( find \ \exists e \in XSLog_{gid}^i \) \( st \ ((\text{rsn-return.rcvr} = e.gid) \wedge (e.ssn = \text{rsn-return.ssn})) \);
  if(\( \neg(\exists o \in e.rsnlist \) \( st \ (\text{rsn-return.rcvr} = o.rcvr)) \)) then
    \( e.rsnlist \leftarrow e.rsnlist \cup \{(\text{rsn-return.rcvr}, \text{rsn-return.rsn})\} \);
  else
    if(\( p_{gid}^i \) has received each a \( rsn \) from every other live member \( p_{gid}^k \in e.gid \)) then
      \textbf{multicast} \( \text{ack}(p_{gid}^i, ssn, e.rsnlist) \) to \( e.gid \);
    else if(\( p_{gid}^i \) has received each a \( rsn \) from every other live member \( p_{gid}^k \in e.gid \)) then
      \( send \ \text{ack}(p_{gid}^i, ssn, e.rsnlist) \) to \( rsn-return.rcvr \);

// When message receiver \( p_{gid}^i \) receives an acknowledgement \( \text{ack} \) from message sender \( \text{ack.sndr} \) indicating the latter has fully logged the corresponding message in its volatile storage and collected the list of \( rsn \)s all other live group members have each assigned for the message. //
Module RCV-ACK(ack(sndr, ssn, rsnlist)) AT \( p_{gid}^i \)
  \( find \ \exists e \in \text{ack.rsnlist} \) \( st \ (e.rcvr = p_{gid}^i) \);
  if(\( \text{stableRSN}_{gid}^i < e.rsn \)) then
    \( find \ \exists o \in XRLog_{gid}^i \) \( st \ (o.sndr = \text{ack.sndr}) \wedge (o.ssn = \text{ack.ssn}) \);
    \( o.rsnlist \leftarrow o.rsnlist \);
    \( allow \ all \ the \ send \ message \ operations \ delayed \ before \ receiving \ the \ message \ whose \ rsn \ value \ is \ (\text{ack.ssn} + 1) \) \( to \ begin \ executing \);
    \( \text{stableRSN}_{gid}^i \leftarrow e.rsn \);

// When process \( p_{gid}^i \) takes its local checkpoint on the stable storage. //
Module TAKE-CHECKPOINT() AT \( p_{gid}^i \)
  \( take \ its \ local \ checkpoint \ with \ (RSN_{gid}^i, SSN_{gid}^i, SsnVt_{gid}^i, XSLog_{gid}^i) \ on \ the \ stable \ storage \);
  \( allow \ all \ the \ send \ message \ operations \ delayed \ before \ this \ checkpoint \ to \ begin \ executing \);
  \( \text{stableRSN}_{gid}^i \leftarrow RSN_{gid}^i \);

Fig. 8. Our group-based SBML procedures during failure-free operation.
// When process $p_{gid}^i$ attempts to recover after failure. //
Module RECOVERY() AT Recovering Process $p_{gid}^i$
  
  restore a latest checkpointed state with ($RSN_{gid}^i$, $SSN_{gid}^i$, $SsnV_{gid}^i$, $XSLog_{gid}^i$) from stable storage;
  
  multicast each a recovery request $rqt-rcvy(p_{gid}^i)$ to group gid;

// $p_{gid}^i$ collects all recovery information of fully or partially logged messages from the other live processes. //
while recovery replies aren’t received from all other group members do
  
  put fully logged messages for $p_{gid}^i$ piggybacked on each reply $rpy-rcvy$ into $flog_{gid}^i$ in RSN order;
  
  put partially logged messages for $p_{gid}^i$ piggybacked on each reply $rpy-rcvy$ into $plog_{gid}^i$ in FIFO order;

// $p_{gid}^i$ replays every fully logged message in $flog_{gid}^i$ in its rsn order like in $p_{gid}^i$’s pre-failure state. //
for all $e \in flog_{gid}^i$ st ($\exists o \in e.rsnlist: (o.rcvr = p_{gid}^i) \land (o.rsn = RSN_{gid}^i+1)$) do
  
  $RSN_{gid}^i \leftarrow RSN_{gid}^i + 1$;
  
  $SsnV_{gid}[e.sndr] \leftarrow e.ssn;
  
  $XRLog_{gid}^i \leftarrow XRLog_{gid}^i \cup \{(e.sndr, e.ssn, e.rsnlist)\}$;
  
  deliver $e.data$ to its corresponding application;
  
  $flog_{gid}^i \leftarrow flog_{gid}^i - \{e\}$;
  
  $stableRSN_{gid}^i \leftarrow RSN_{gid}^i$;

// $p_{gid}^i$ replays every partially logged message in $plog_{gid}^i$ in FIFO order like in $p_{gid}^i$’s pre-failure state. //
while $plog_{gid}^i$ is a non-empty set do
  
  randomly select $\exists e$ in $plog_{gid}^i$ st ($e.ssn = SsnV_{gid}[e.sndr]+1$);
  
  call Module G-RECV($e.sndr, e.ssn, e.data$) at $P_{gid}^i$;
  
  $plog_{gid}^i \leftarrow plog_{gid}^i - \{e\}$;

// When a surviving process $p_{gid}^i$ receives a recovery message $rqt-rcvy$ from another process $p_{rcvy}.rcvr$ requesting the log information for recovery of every process including the latter from $p_{gid}^i$’s volatile storage. //
Module RCV-RQTRCVY($rqt-rcvy(rcvr)$) AT Live Process $p_{gid}^i$
  
  put fully and partially logged messages for $rqt-rcvy.rcvr$ in $XSLog_{gid}^i$ and $XRLog_{gid}^i$ into a reply $rpy-rcvy$;
  
  send $rpy-rcvy$ to $rqt-rcvy.rcvr$;

Fig. 9. Recovery and its assisting procedures.

5. CORRECTNESS PROOF

This section proves our proposed SBML protocol ensures system consistency in case of concurrent failures using one lemma and one theorem.
Lemma 1. Our proposed protocol always prevents every failed process $P_g^i$ in group $g$ from making any other live process in group $g$ orphan process.

Proof. Suppose the set of all the fully logged messages $P_g^i$ has received before its failure is denoted by $\text{FULLY-LOGGED-MSGs}_{g,i}$. The proof proceeds by induction on the number of all the messages in $\text{FULLY-LOGGED-MSGs}_{g,i}$, denoted by $\text{NUMOF}(\text{FULLY-LOGGED-MSGs}_{g,i})$.

[Base case] In this case, there is one fully logged message $m$ to group $g$ $P_g^i$ has received before its failure and there are two cases we should consider.

Case 1: m’s sender $P_g^s$ is a surviving process.

In this case, $P_g^s$ can trivially give $P_g^i$ all rsns of $m$ from $\text{SndLg}_g^s$ all the other processes in group $g$ including $P_g^i$ have assigned to $m$ before. So, $P_g^i$ can put them into $\text{GRsnLg}_g^i$ and then, replay $m$ in $m$’s original order like in its pre-failure state. Therefore, no surviving process that has received any message sent from $P_g^i$ after $m$’s receipt becomes orphan process.

Case 2: m’s sender $P_g^s$ has failed.

In this case, there are two sub-cases we should consider.

Case 2.1: there is no surviving process in group $g$.

In this case, even although $P_g^i$ replays $m$ in any order unlike in its pre-failure state, no inconsistency problem will occur in the system because there is no orphan state on which $m$’s receive event occurrence before its failure has any impact.

Case 2.2: there is at least one surviving process $P_g^j$ in group $g$.

In this case, as message $m$ has been fully logged, m’s sender $P_g^s$ before failure transmitted all surviving processes including $P_g^j$ all rsns of $m$ from $\text{SndLg}_g^s$ all the other processes in group $g$ including $P_g^i$ had assigned to $m$ before. So, $P_g^i$ can get the rsns from $\text{GRsnLg}_g^j$ of $P_g^j$ and put them into $\text{GRsnLg}_g^i$, and then replay $m$ in $m$’s original order like in its pre-failure state by obtaining $m$’s data from recovering $P_g^s$. Therefore, $P_g^i$’s failure never makes any surviving process that has received any message sent from $P_g^i$ after $m$’s receipt orphan process.

[Induction hypothesis]

We assume that the theorem is true for $P_g^i$ in case that $\text{NUMOF}(\text{FULLY-LOGGED-MSGs}_{g,i})=k$.

[Induction step]

By induction hypothesis, $P_g^i$ can get all the log information of $k$ fully logged messages it has received before its failure. Therefore, if $P_g^i$ can take the log information of $(k+1)$-th message fully logged before its failure in this recovery procedure, the theorem is true for $P_g^i$ in case $\text{NUMOF}(\text{FULLY-LOGGED-MSGs}_{g,i})=k+1$. The following case is similar to the base case stated above.
By the induction, among the lost state intervals of every failed process, all those that any normally operational process’s state depends on can always be recovered by performing the proposed protocol.

**Theorem 1.** Even if \( k (1 < k \leq n) \) processes in a process group of size \( n, g \), crash concurrently, our proposed protocol allows consistent recovery to be able to be completed.

**Proof.** We prove this theorem by contradiction. Assume that our protocol may not make consistent recovery possible to be successfully finished in case of \( k \) simultaneous process failures. Suppose the set of all failed processes in group \( g \) is denoted by SET-OF-FAILEDPROCS\(_g\) and the set of all surviving processes in group \( g \), SET-OF-SURPROCS\(_g\). There are two process failure cases to consider as follows:

**Case 1:** there is no surviving process in group \( g \) (\( k = n \)).

In this case, there occurs no orphan state interval, meaning every recovering process can replay each received message in a new order without considering the current state interval of any normally operational process.

**Case 2:** there are one or more surviving processes in group \( g \) (\( 1 < k < n \)).

This case means there is at least one orphan state interval their current states depend on directly or indirectly. This set of orphan state intervals can be classified into two kinds: state intervals directly created by the messages sent by any failed processes, SET-OF-DIROSI\(_g\)s, and directly created by the messages sent by any other surviving processes, SET-OF-INDIROSI\(_g\)s.

In this case, there are two sub-cases to consider:

**Case 2.1:** Any state interval \( s_i \in \text{SET-OF-DIROSI}_g \) is created by the receive event of message \( m \).

In this case, suppose \( s_i \) is created by receive\(_g^i\)(\( m \)) at \( P_g^i \in \text{SET-OF-SURPROCS}_g \) and depends on the receive events of all the messages \( P_g^i \) has received until generating \( s_i \). Even though all the senders of the received messages, denoted by DirectMsgsSenders\(_g(s_i)\), would be a subset of SET-OF-FAILEDPROCS\(_g\), by lemma 1, \( s_i \) never becomes an orphan state because the proposed protocol forces no crashed process in DirectMsgsSenders\(_g(s_i)\) to make \( P_g^i \) be an orphan process.

**Case 2.2:** Any state interval \( s_i \in \text{SET-OF-INDIROSI}_g \) is created by the receive event of message \( m \).

In this case, if \( s_i \) depends transitively on any state interval \( s_i' \in \text{SET-OF-DIROSI}_g \), it may be an orphan state if \( s_i' \) could not be restored even after having completed the recovery procedure. But, this situation cannot occur according to case 2.1.

Therefore, consistent recovery is possible in all the cases. This contradicts the hypothesis.
6. ANALYSIS

This section presents some numerical analysis results to compare our proposed SBML protocol (OURS) to the original one with RSN replication functionality for ensuring no rollback of surviving processes (ORIGIN-REP) [3, 10, 14, 25] regarding control message exchange overhead during failure-free operation. Here, as ORIGIN-REP is designed based on unicast communication links for enabling RSN replication, if a group size is k, it requires that k individual control messages from each message sender should be sent to all group members.

For this purpose, several parameters used are defined as follows:

- $N_{\text{proc}}$: the total number of processes in a group.
- $N_{\text{appmsg}}$: the total number of application messages generated in a group.
- $C_{\text{multi}}$: the cost of sending a multicast message to every member in a group.
- $C_{\text{uni}}$: the cost of sending a unicast message to an individual process.

In this evaluation, we assume a computer cluster of $N_{\text{proc}}$ processes or nodes with two different one-way message costs, $C_{\text{uni}}$ and $C_{\text{multi}}$. With this assumed model, the total control message costs of ORIGIN-REP and OURS occurring during failure-free operations, denoted by $\text{ORIGIN-REP}_{\text{msg-cost}}$ and $\text{OURS}_{\text{msg-cost}}$, can be expressed as Eq. 1 and Eq. 2 respectively.

\[
\text{ORIGIN-REP}_{\text{msg-cost}} = 2 \times C_{\text{uni}} \times (N_{\text{proc}} - 1) \times N_{\text{appmsg}} \tag{1}
\]

\[
\text{OURS}_{\text{msg-cost}} = (C_{\text{uni}} \times (N_{\text{proc}} - 1) + C_{\text{multi}}) \times N_{\text{appmsg}} \tag{2}
\]

The difference of control message costs of ORIGIN-REP and OURS, $\Delta \text{DIFF}_{\text{msg-cost}}$ (= Eq. 1 – Eq. 2), is Eq. 3.

\[
\Delta \text{DIFF}_{\text{msg-cost}} = (C_{\text{uni}} \times (N_{\text{proc}} - 1) - C_{\text{multi}}) \times N_{\text{appmsg}} \tag{3}
\]

From Eq. 3, we can see that $\Delta \text{DIFF}_{\text{msg-cost}}$ may linearly become larger as the number of messages generated increases and the difference between $C_{\text{multi}}$ and $C_{\text{uni}}$ decreases. In general, a multicast sending ($C_{\text{multi}}$) is highly more efficient than achieving an equivalent job using unicast only send primitive ($C_{\text{uni}} \times (N_{\text{proc}} - 1)$) in most LAN or WAN-based multicast protocols developed in network or application layers. Thus, as $N_{\text{proc}}$ increases, $\Delta \text{DIFF}_{\text{msg-cost}}$ may also be higher.

Let us clarify how much OURS may reduce the control message overhead of the entire system during failure-free operation compared with ORIGIN-REP using Fig. 10 and 11. The two figures show the variation of reduction rate, $\text{Rate}_{\text{msg-cost}}$ of $\text{OURS}_{\text{msg-cost}}$ against $\text{ORIGIN-REP}_{\text{msg-cost}}$ with varying $N_{\text{proc}}$ ranging from 10 to 50 in case $\rho (= C_{\text{multi}} / C_{\text{uni}})$
$C_{uni}$ is 1.0 through 4.5 at 0.5 intervals. The reduction rate is expressed as $\Delta DIFF_{msg-cost} / ORIGIN-REP_{msg-cost}$. In these figures, as $N_{proc}$ becomes bigger, their $Rate_{msg-cost}$s appear to be converging very close to 0.5. Especially, as $\rho$ becomes close to 1, i.e., the difference between two one-way communication costs, $C_{mult}$ and $C_{uni}$, is smaller, the $Rate_{msg-cost}$ begins from much higher value. This outcome arises from the reason that the increase of the number of processes in a group and the decrease of $\rho$ allows OURS to enormously lower the number of control messages between processes in a group during failure-free operation compared with ORIGIN-REP. In particular, if most of the physical network types used in a cluster are broadcast, OURS can reduce very close to 50% of the total control message cost of ORIGIN-REP.

In conclusion, these results show that our SBML protocol using the beneficial features of FIFO broadcast links remarkably lowers the cost of additional inter-process communication of the original SBML required for ensuring no rollback of surviving processes while being capable of tolerating concurrent failures without any inconsistency problem.

![Graph](image_url)

**Fig. 10.** $Rate_{msg-cost}$ with varying values of $N_{proc}$ and $\rho$. 
7. EVALUATION

In this section, we perform extensive simulations to measure the RSN replication overhead of our proposed SBML protocol (OURS) against the original one based on group communication without RSN replication functionality (ORIGIN-GC-NOREP) using a discrete-event simulation language [28]. Two performance indicators are used for comparison; the elapsed time until the same distributed execution has been completed (T_{complete}), and the increasing rate of the performance overhead of the two protocols for simultaneous failures against the original SBML, ORIGIN, for only tolerating a single failure at a time (IncreaseOverhead). A system with N nodes connected through a general network is simulated. Each node has one process executing on it and, for simplicity, the processes are assumed to be initiated and completed together. Each process group consists of three processes and the number of process groups (NOG) is 10, 15, 20, 25, 30 and 35 (N=30, 45, 60, 75, 90, 105). Here, the degree of RSN redundancy of OURS, k, is configured to 3. The target of each message sent from a process is always a process group. Thus, IP multicast is used for multicasting a message to a group of processes. The message transmission capacity of a link in the network is 100Mbps and its propagation delay is 1ms. Every process has a 128MB buffer space for storing its message log. The message size ranges from 1KB to 1MB. Normal checkpointing is initiated at each process with an interval following an exponential distribution with a mean $T_{nc} = 300$ seconds. In addition, a message to a process group is sent from a randomly chosen process with an interval following an exponential distribution with a mean of $T_{ms}=3$ seconds. All experimental results shown in this simulation are all averages over a number of trials.

Distributed applications used for the simulation exhibit the following four communication patterns, respectively [27].
• Serial pattern: All process groups are organized in a serial manner and transfer messages for one way. When a process group, except the first and the last ones, receives a message from its predecessor, it sends a message to its successor, and vice versa. The first process group communicates with only its successor and the last one communicates with its predecessor only.

• Circular pattern: A logical ring is structured for communication among process groups in this pattern. Every process group communicates with only two directly connected neighbors.

• Hierarchical pattern: A logical tree is structured for communication among process groups in this pattern. Every process group, except one root group, communicates with only one parent process group and k child process groups (k ≥ 0). The root group communicates with its child group only.

• Irregular pattern: The communication among process groups follows no special communication pattern. Here, a message to a process group is sent from a randomly chosen process group.

Fig. 12 shows T\textsubscript{complete} for the two protocols, OURS and ORIGIN-GC-NOREP, for four different communication patterns respectively with varying the number of process group (NOG) in case the group size is 3. As NOG becomes bigger, T\textsubscript{complete} of the two protocols also increases because their inter-group communication costs are higher. Also, T\textsubscript{complete} of OURS is larger than T\textsubscript{complete} of ORIGIN-GC-NOREP because the RSN delivery time of the first may be longer during its RSN replication procedure compared with the latter. However, this simulation results indicate the difference between T\textsubscript{complete}s of the two protocols ranges only from 3.2% through 7.9% of the latter regardless of application communication patterns.

Fig. 13 shows the average values of Increase\textsubscript{Overhead} of the two protocols, ORIGIN-GC-NOREP and OURS, for the four communication patterns when the number of simultaneous failures is 2. As NOG becomes bigger, their Increase\textsubscript{Overhead} values are also increasing. This phenomenon arises from the reason that the increase of NOG leads to the higher interaction overhead resulting from the RSN replication procedure. But, this simulation results illustrate the differences in Increase\textsubscript{Overhead} values in both protocols grow as the value of NOG increases. Especially, in the entire range, Increase\textsubscript{Overhead} of OURS is greater than that of ORIGIN-GC-NOREP rising up to 8.9%, but becomes less than 15% even when NOG is 35. From this outcome, it may be claimed that our protocol incur the reasonable performance overhead against ORIGIN in order to tolerate simultaneous failures in this range.

From these results, we can see that OURS can be a low cost solution for addressing the critical limitation of ORIGIN-GC-NOREP, i.e., capable of masking sequential failure only.
SBML protocol for conquering simultaneous failures with group dissemination

Fig. 12. Comparisons of $T_{\text{complete}}$ of the two protocols with varying values of NOG: (a) Serial Pattern; (b) Circular Pattern; (c) Hierarchical Pattern; (d) Irregular Pattern.

Fig. 13. Comparisons of IncreaseOverhead of the two protocols with varying values of NOG.
8. CONCLUSIONS

In group communication link-based distributed systems, the presented protocol can overcome the constraint on simultaneous failures by enabling every process to maintain the respective RSN of each same message assigned by every other live group member onto its own volatile memory. With this beneficial feature, it allows the system to survive a number of simultaneous failures except the whole system failure. Also, achieving the feature causes no extra control message by piggybacking the additional information on the control message for logging every previous protocol essentially needs. However, this feature may cause the time, which has elapsed until releasing the stalled messages, to be a little longer. But, the control message including the different RSNs of each message needs to be multi-casted to a group at once in our protocol whereas if the group size is k, the original SBML with RSN replication functionality requires that k individual control messages from its sender should be sent to all group members. The analysis and simulation results show that the proposed protocol can be a lightweight fault-tolerance technique for addressing the critical limitation of the original one based on group communication without RSN replication functionality, i.e., capable of masking sequential failure only.

For future works, we attempt to extend the proposed protocol to be able to handle the overlapping group communication in an effective manner.

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